## .RTHA INSTITUTE OF SCIENCE AND TECHNOLOGY :: PUTTUR

Siddharth Nagar, Narayanavanam Road - 517583

## QUESTION BANK (DESCRIPTIVE)

## Subject with Code : Transform \& Discrete Mathematics (18HS0832)

## Course \& Branch : B.Tech CE

Year \&Sem : II-B.Tech\& I-Sem
Regulation : R18

## UNIT-I

## TRANSFORM CALCULUS-I

1. a) Find theLaplace transform of $e^{a t} \cosh b t$
b) Find the Laplace transform of $3 \cos 3 t \cdot \cos 4 t$
c) Find $L^{-1}\left\{\frac{2 s-5}{4 s^{2}+25}\right\}$ by using linear property.
d) Find $L\left\{t^{2}+3 t+10\right\}$
e) State Convolution theorem.
2. a) Find the Laplace transform of $e^{-3 t}(2 \cos 5 t-3 \sin 5 t)$
b) Find the Laplace transform of $f(t)=\int_{0}^{t} e^{-t} \cos t d t$.
3. a) Find the Laplace transform of $f(t)=\frac{1-\cos a t}{t}$
b) Show that $\int_{0}^{\infty} t^{2} e^{-4 t} \cdot \sin 2 t d t=\frac{11}{500}$,Using Laplace transform
4. a)Find Laplace Transform of Square-wave function of periodic 2 a ,
defined as $f(t)=\left\{\begin{array}{rr}k, & 0<t<a \\ -k, & a<t<2 a\end{array}\right.$
b) Using Laplace transform, evaluate $\int_{0}^{\infty} \frac{\cos a t-\cos b t}{t} d t$.
5. a) Find the Laplace transform of $f(t)=e^{-4 t} \int_{0}^{t} \frac{\sin 3 t}{t} d t$.
b) Find the Laplace transform of $f(t)=t e^{2 t} \sin 3 t$
6. a) Find $L^{-1}\left\{\frac{3 s-2}{s^{2}-4 s+20}\right\}$ by using first shifting theorem
b) Find $L^{-1}\left\{\frac{1}{2} \log \left(\frac{s^{2}+a^{2}}{s^{2}+b^{2}}\right)\right\}$
7. a) Find $L^{-1}\left\{\frac{1}{\left(s^{2}+5^{2}\right)^{2}}\right\}$, using Convolution theorem.
b) Find $L^{-1}\left\{\frac{s^{2}}{\left(s^{2}+4\right)\left(s^{2}+25\right)}\right\}$,using Convolution theorem.
8. a) Find the Inverse Laplace transform of $\frac{1}{s^{2}\left(s^{2}+a^{2}\right)}$.
b)Find $L^{-1}\left\{\log \left(\frac{s-1}{s+1}\right)\right\}$
9. Use transform method to solve $\left(D^{2}+5 D+6\right) y=5 e^{t}$ where $y(0)=2, y^{1}(0)=1$
10. Solve the D.E $\frac{d^{2} y}{d t^{2}}+2 \frac{d y}{d t}+2 y=5 \sin t$ using Laplace Transform given that $y(0)=0, y^{1}(0)=0$

## UNIT II

## Fourier Transforms

1. a) Find the Fourier sine transform of $e^{-|x|}$ Hence show that $\int_{0}^{\infty} \frac{x \sin m x}{1+x^{2}} d x=\frac{\pi}{2} e^{-m}, m>0$.
b) Find the Fourier cosine transform of $2 e^{-5 x}+5 e^{-2 x}$.
2. Find the Fourier transform of $f(x)= \begin{cases}a^{2}-x^{2}|x|<a \\ 0 & |x|>a>0\end{cases}$

Hence show that $\int_{0}^{\infty} \frac{\sin x-x \cos x}{x^{3}} d x=\frac{\pi}{4}$.
3. a) Find the Fourier transform of $f(x)=e^{\frac{-x^{2}}{2}},-\infty<x<\infty$
b) If $\mathrm{F}(p)$ is the complex Fourier transform of $\mathrm{f}(x)$, then prove that the complex fourier transform of $\mathrm{f}(x) \cos x a$ is $\frac{1}{2}\left[F_{s}(p+a)+F_{s}(P-a)\right]$.
4. a) Find the Fourier cosine transform of $e^{-a x} \cos a x, a>0$.
b) Find the Fourier cosine transform of $f(x)=\left\{\begin{array}{cc}x & \text { for } 0<x<1 \\ 2-x & \text { for } 1<x<2 . \\ 0 & \text { for } x>2\end{array}\right.$
5. Find the Fourier sine and cosine transforms of $f(x)=\frac{e^{-a x}}{x}$ and deduce that

$$
\int_{0}^{\infty} \frac{e^{-a x}-e^{-b x}}{x} \sin s x d x=\tan ^{-1}\left(\frac{s}{a}\right)-\tan ^{-1}\left(\frac{s}{b}\right)
$$

6. Find the Fourier sine and cosine transforms of $f(x)=e^{-a x}, a>0$ and hence deduce the integrals $(i) \int_{0}^{\infty} \frac{p \sin p x}{a^{2}+p^{2}} d p(i i) \int_{0}^{\infty} \frac{\cos p x}{a^{2}+p^{2}} d p$
7. Find the Inverse Fourier sine transform of $f(x)$ of $F_{s}(p)=\frac{p}{1+p^{2}}$.
8. a) Find the finite Fourier sine transform of $f(x)=\left\{\begin{array}{ll}x, & 0 \leq x \leq \frac{\pi}{2} \\ \pi-x, & \frac{\pi}{2} \leq x \leq \pi\end{array}\right.$.
b) Find the inverse finite Fourier sine transform of $f(x)$, if $F_{S}(n)=\frac{16(-1)^{n-1}}{n^{3}}$, where n is a positive integer and $0<x<8$.
9. a)Find the Finite cosine transform of $f(x)=e^{a x}$ in $(0, l)$.
b) Find the Inverse Fourier cosine transform $f(x)$ if $F_{c}(n)=\frac{\cos \left(\frac{2 n \pi}{3}\right)}{(2 n+1)^{2}}$ where $0<x<4$.
10. a) Write the Inversse Fourier Transform.
b) Show that $F_{s}\{x f(x)\}=-\frac{d}{d s}\left\{F_{c}(s)\right\}$.
c) Write the formula for Finite Fourier cosine transform.
d) Find the Inverse Fourier sine transform $\mathrm{f}(\mathrm{x})$ if $F_{S}(n)=\frac{1-\cos n \pi}{n^{2} \pi^{2}} 0<x<\pi$.
e) Find the Fourier transform of $f(x)$ defined by $f(x)=\left\{\begin{array}{rr}0 & -\infty<x<\alpha \\ x & \alpha<x<\beta \\ 0 & x>\beta\end{array}\right.$

## UNIT-III

## ALGEBRAIC STRUCTURES

1. Define group and an abelian group. Prove that the set $Z$ of all integers with the binary operation *, defined as $a * b=a+b+1, \forall a, b \in Z$ is an abelian group.
2. a)Define and give an examples for group, semi group, subgroup \&abelian group.
b)Let $\mathrm{s}=\{\mathrm{a}, \mathrm{b}, \mathrm{c}\}$ and let *denotes a binary operation on 's' is given below also let $\mathrm{p}=\{1,2,3\}$ and addition be a binary operation on ' p ' is given below. show that $\left(\mathrm{s},{ }^{*}\right) \&(\mathrm{p},(+)$ ) are isomorphism

| $*$ | A | B | C |
| :--- | :--- | :--- | :--- |
| A | A | B | C |
| B | B | B | C |
| C | C | B | C |


| $(+)$ | 1 | 2 | 3 |
| :--- | :--- | :--- | :--- |
| 1 | 1 | 2 | 1 |
| 2 | 1 | 2 | 2 |
| 3 | 1 | 2 | 3 |

3. a)Show that the set $=\{1,2,3,4,5\}$ is not a group under addition \& multiplication modulo 6
b) On the set Q of all rational number operation * is defined by $\mathrm{a} * \mathrm{~b}=\mathrm{a}+\mathrm{b}-\mathrm{ab}$.

Show that this operation Q forms a commutative monoid.
4. a) Explain the concepts of homomorphism and isomorphism of groups with examples.
b) $\operatorname{Let}(G, *)$ and $(H, \Delta)$ be a groups and $g: G \rightarrow H$ be a homomorphism. The the kernerl of g is a normal subgroup.
5 a)The necessary and sufficient condition for a non-empty sub-set H of a Group (G,*) to be a sub group is $\mathrm{a} \epsilon \mathrm{H}, \mathrm{b} \in \mathrm{H}=>\mathrm{a}^{*} \mathrm{~b}^{-1} \mathrm{CH}$
b) Show that every homomorphic image of an abelian group is abelian.
6. a) Show that the set of all roots of the equation $x^{4}=1$ forms a group under multiplication.
b) Showthat the set of all rational numbers forms an abelian group under the composition defined by

$$
a * b=\frac{a b}{2}
$$

7. a) In a group $G$ for $a, b \in G, o(a)=5, b \neq e$ and $a b a^{-1}=b^{2}$. Show that $o(b)=31$.
b) Let $s=\{a, b\}$ be a set consider all possible permutations of $S$ as $s_{2}=\left\{P_{1}, P_{2}\right\}$ Show that $\left(s_{2}, *\right)$ is a permutation group.
8. a) Let $Z_{5}^{*}=\{[1],[2],[3],[4]\}$ in which [1], [2], .... have the same meaning as in $Z_{5}$ except that $Z_{5}^{*}=Z_{5}-\{[0]\}$. Also let $X_{5}$ is multiplication modulo 5. Show that $g: Z_{4} \rightarrow Z_{5}^{*}$ is given by $g([0])=[1], g([1])=[2], g([2])=[4], g([3])=[3]$ defines a homomorphism from the group $\left(Z_{4},+_{4}\right)$ to $\left(Z_{5}^{*}, *_{4}\right)$.Hence show that $g$ is group isomorphic.
b) Show that if $a, b$ are arbitrary elements of a group $G$ then $(a b)^{2}=a^{2} b^{2}$ iff $G$ is abelian.
9. a) Prove that the order of a subgroup of a finite group divides the order of the group ?
b) Prove that the kernel of a homomorphism from ( $\mathrm{G},{ }^{*}$ ) to ( $\mathrm{H}, \Delta$ ) is a subgroup of ( $\mathrm{G},{ }^{*}$ ) .
10.(a) Define Monoid, Semi group?
(b) Let $\left(Z_{4}+_{4}\right) G=\{1,-1, i,-i\}$ be a multiplicative group. Find the order of every element.
(c) Define isomorphism of a group?
(d) Define Normal group?
(e) Define Homomorphism of a semi group?

## UNIT IV

## Introduction to counting

1. (a)In how many ways can a committee of 5 teachers and 4 students be chosen from 9 teachers and 15 students with at least 2 students in each committee ?
(b) How many integral solutions are there to $x_{1}+x_{2}+x_{3}+x_{4}+x_{5}=20$ where
(i) each $x_{i} \geq 2$ ?
(ii) each $\mathrm{x}_{\mathrm{i}}>2$ ?
2. (a) How many numbers can be formed using the digits $1,3,4,5,6,8$ and 9 if no Repetitionsare allowed?
(b) Find the generating function for the sequence $1,1,1,3,1,1, \ldots \ldots \ldots \ldots$
3. (a) The question paper of mathematics contains two questions divided into two groups of 5 questions each. In how many ways can an examine answer six questions taking at least two questions from each group.
(b) How many permutations can be formed out of the letters of word "SUNDAY"? How many of these (i) Begin with S? (ii) end with Y? (iii) begin with S \& end with Y ? (iv) S \& Y always together ?
4. (a) In how many ways can the letters of the word COMPUTER be arranged? How many of them begin with C and end with R ? How many of them do not begin with C but end with R ?
(b) out of 9 girls and 15 boys how many different committees can be formed each consisting of 6 boys and 4 girls?
5. a) Determine the number of positive integer $1 \leq n \leq 100$ and is not divisible by 2,3 , or 5
b) Solve $a_{n}=a_{n-1}+2 a_{n-2}, n \geq 2$ with initial conditions $a_{0}=0, a_{1}=1$
6. a) Solve $a_{n}=3 a_{n-1}-3 a_{n-2}+a_{n-3}$ with initial conditions $a_{0}=0, a_{3}=3, a_{5}=10$
b) A survey among 100 students shows that of the three ice cream flavors vanilla, chocolate, strawberry 50 students like vanilla, 43 like chocolate, 28 like straw berry, 13 like vanilla and chocolate, 11 like chocolate and straw berry, 12 like straw berry and vanilla and 5 like all of them. Find the following.
7. (a) Find how many integers between 1 and 60 that are divisible by 2 nor by 3 and nor by 5 . Also determine the number of integers divisible by 5 not by 2 , not by 3 .
b) out of 80 students in a class, 60 play football, 53 play hockey, and 35 both the games . how many students (i) do not play of these games. (ii) play only hockey but not football.
8. a) Applying pigeon hole principle show that of any 14 integers are selected from the set $S=\{1,2,3, \ldots \ldots ., 25\}$ there are at least two whose seem is 26 . Also write a statement that generalizes this result.
b) Show that if 8 people are in a room, at least two of them have birthdays that occur on the same day of the week
9. a) Determine the sequence generated by
$f(x)=2 e^{x}+3 x^{2}$
(ii) $7 \mathrm{e}^{8 x}-4 \mathrm{e}^{3 x}$.
b) Solve the RR $a_{n+2}-2 a_{n+1}+a_{n}=2^{n}$ with initial condition $a_{0}=2 \& a_{1}=1$.
10. (a) State Pigeon?
(b) State Multinomial theorem?
(c) Define permutation \& Combination?
(d) State Generating Function?
(e) State Inclusion and Exclusion?

## UNIT-5

## Introduction to Graphs

1. a) Define isomorphism. Explain Isomorphism of graphs with a suitable example.
b) Explain graph coloring and chromatic number give an example.
2. a)Explain about complete graph and planar graph with an example
b) Define the following graph with one suitable example for each graphs
(i) spanning tree
(ii) sub graph
(iii) induced sub graph (iv) spanning sub graph
3. a) Explain In degree and out degree of graph. Also explain about the adjacency matrix representation of graphs. Illustrate with an example?
b) Give an example of a graph that has neither an Eulerian circuit nor a Hamiltonian circuit
4. a) Show that the maximum number of edges in a simple graph with $n$ vertices is $n(n-1) / 2$
b) A graph $G$ has 21 edges, 3 vertices of degree 4 and the other vertices are of degree 3 . Find the number of vertices in G?
5. a) Suppose a graph has vertices of degree $0,2,2,3$ and 9 . How many edges does the graph have ?
b) Give an example of a graph which is Hamiltonian but not Eulerian and vice versa .
6. a) Let G be a 4 - Regular connected planar graph having 16 edges. Find the number of regions of G .
b) Draw the graph represented by given Adjacency matrix

$$
\text { (i) }\left[\begin{array}{llll}
1 & 2 & 0 & 1 \\
2 & 0 & 3 & 0 \\
0 & 3 & 1 & 1 \\
1 & 0 & 1 & 0
\end{array}\right]
$$

(ii) $\left[\begin{array}{llll}0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 1 & 0 & 1 & 0\end{array}\right]$
7. a) Show that in any graph the number of odd degree vertices is even .
b) Is the following pairs of graphs are isomorphic or not?

(b)

8. a) Show that the two graphs shown below are isomorphic?
b) Explain about the Rooted tree with an example?
9. a) (i)Find the chromatic polynomial \& chromatic number for $\mathrm{K}_{3,3}$
(ii) Define Euler circuit, Hamilton cycle ,Wheel graph ?
b) Explain any 5 graphs with examples.
10. a) Define regular graph.
a)State handshaking theorem.
b) Define Complete bipartite graph.
c) State Euler's formula.
d)Determine the number of edges in cycle graph $C_{n}$

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## QUESTION BANK (OBJECTIVE)

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Course \& Branch : B.Tec CE\&AG
Year \&Sem : II-B.Tech\& I-Sem
Regulation : R18

## TRANSFORM CALCULUS-I

1. $L\left\{e^{-a t}\right\}=$
A) $\frac{1}{s^{2}+a^{2}}$
B) $\frac{a}{s^{2}+a^{2}}$
C) $\frac{1}{s+a}$
D) $\frac{1}{s-a}$
2. $L\{\operatorname{Cos} a t\}=$
A) $\frac{s}{s^{2}+a^{2}}$
B) $\frac{a}{s^{2}+a^{2}}$
C) $\frac{1}{s+a}$
D) $\frac{1}{s-a}$
3. $L\{2\}=$
A) $\frac{1}{s}$
B) $\frac{2}{s}$
C) $\frac{1}{s^{2}}$
D) 1
4. $L\{$ Coshat $\}=$
A) $\frac{s}{s^{2}-a^{2}}$
B) $\frac{a}{s^{2}+a^{2}}$
C) $\frac{1}{s+a}$
D) $\frac{s}{s^{2}+a^{2}}$
5. $L\left\{e^{a t} \sin b t\right\}=$
A) $\frac{s}{(s-a)^{2}+b^{2}}$
B) $\frac{s}{(s-a)^{2}-b^{2}}$
C) $\frac{b}{(s-a)^{2}+b^{2}}$
D) $\frac{b}{(s-a)^{2}-b^{2}}$
6. If $L\{f(t)\}=f(s)$ then $L\left\{e^{-a t} f(t)\right\}=$
A) $\bar{f}(s+a)$
B) $\bar{f}(s-a)$
C) $\bar{f}(a s)$
D) $(s+a)$
7. The Laplace transform of $f(t)$ is defined as
A) $\int_{0}^{\infty} e^{-s t} f(t) d t$
B) $\int_{0}^{\infty} e^{-s t} f \bar{f}(s) d t$
C) $\int_{0}^{\infty} e^{s t} f(t) d t$
D) None
8. If $L^{-1}\left\{\frac{1}{s-2}\right\}=$
A) $\frac{e^{-a t}}{s}$
B) $\frac{3 e^{-a t}}{2}$
C) $e^{2 t}$
D) $\frac{e^{-2 s}}{2}$
9. $L\{\sinh a t\}=$
A) $\frac{s}{s^{2}-a^{2}}$
B) $\frac{a}{s^{2}+a^{2}}$
C) $\frac{1}{s+a}$
D) $\frac{a}{s^{2}-a^{2}}$
10. Find the value of $L^{-1}\left\{\frac{s^{2}+3 s+7}{s^{3}}\right\}=$ $\qquad$ .
A) $1-3 t-\frac{7}{2} t^{2}$
B) $1+3 t+\frac{7}{2} t^{2}$
C) $1-3 t-7 t^{2}$
D) None
11. $L\{k\}=$
A) $\frac{k}{s}$
B) $\frac{1}{s}$
C) $\frac{1}{s^{2}}$
D) $k$
12. The value of $L^{-1}\left\{\frac{1}{s}\right\}=$
(A) 1
B) 0
C) -1
D)None
13. $L\left\{e^{a t}\right\}=$
A) $\frac{1}{s^{2}+a^{2}}$
B) $\frac{a}{s^{2}+a^{2}}$
C) $\frac{1}{s+a}$
D) $\frac{1}{s-a}$
14. $L\left\{e^{a t} t^{2}\right\}=$
A) $\frac{a}{(s-a)^{2}}$
B) $\frac{a}{(s-a)^{3}}$
C) $\frac{2}{(s-a)^{3}}$
D) $\frac{3}{(s+a)^{3}}$
15. $L\left\{e^{a t} \cos a t\right\}=$
A) $\frac{s-a}{(s-a)^{2}+b^{2}}$
B) $\frac{s-b}{(s-a)^{2}-b^{2}}$
C) $\frac{b}{(s-a)^{2}+b^{2}}$
D) $\frac{b}{(s-a)^{2}-b^{2}}$
16. If $L\{f(t)\}=f(s)$, then $L\left\{\frac{f(t)}{t}\right\}=$
A) $\int_{s}^{\infty} \bar{f}(s) d s$
B) $\int_{-\infty}^{\infty} \bar{f}(s) d s$
C) $\int_{-\infty}^{\infty} \bar{f}(t) d s$
D) $\int_{0}^{\infty} \bar{f}(s) d s$
17. If $L\{f(t)\}=\bar{f}(s)$,then $L\left\{e^{a t} f(t)\right\}$ $\qquad$
A) $\bar{f}(s)$
B) $\bar{f}(s-a)$
C) $\bar{f}(s+a)$
D) None
18. If $L^{-1}\left\{\frac{4}{s-3}\right\}=$
A) $\frac{e^{-a t}}{s}$
B) $\frac{3 e^{-a t}}{s}$
C) $4 e^{3 t}$
D) $\frac{e^{-a s}}{s}$
19. The value of $L^{-1}\left\{\frac{1}{(S+a)^{5}}\right\}$ is
A) $e^{-a t} \frac{t^{4}}{24}$
B) $e^{a t} t^{4}$
C) $e^{a t} \frac{t^{4}}{24}$
D) $e^{-a t} t^{4}$
20. If $L\{f(t)\}=\bar{f}(s)$, then $L\{f(a t)\}$ $\qquad$ -.
A) $a \bar{f}(s)$
B) $\frac{1}{a} \bar{f}\left(\frac{s}{a}\right)$
C) $\bar{f}\left(\frac{s}{a}\right)$
D) None
21. $L\{\cosh 3 t\}=$
A) $\frac{s}{s^{2}+3^{2}}$
B) $\frac{a}{s^{2}-3^{2}}$
C) $\frac{1}{s^{2}+3^{2}}$
D) $\frac{s}{s^{2}-3^{2}}$
22. Find $L\left\{e^{t} \sin t\right\}=$ $\qquad$ _.
A) $\frac{1}{s^{2}+1}$
B) $\frac{1}{s^{2}-1}$
C) $\frac{s}{s^{2}+1}$
D) $\frac{1}{(s-1)^{2}+1}$
23. Find the value of $L\left\{t^{3}+6\right\}=$ $\qquad$ .
A) $\frac{3}{s^{2}}+\frac{6}{s}$
B) $\frac{6}{s^{4}}+\frac{6}{s}$
C) $\frac{3}{s^{2}}-\frac{6}{s}$
D) None
24. If $L^{-1}\left\{\frac{s}{s^{2}-2^{2}}\right\}=$
(A) $\frac{1}{2} \sinh 2 t$
B) $\frac{1}{2} \cos 2 t$
C) $\sin 2 t$
D) $\cosh 2 t$
25. Find the value of $L^{-1}\left\{\frac{1}{(s-a)^{5}}\right\}=$ $\qquad$ .
A) $e^{a t} t^{4}$
B) $e^{a t} t^{4} / 4$
C) $e^{a t} \frac{t^{4}}{4!}$
D) $\frac{t^{4}}{4!}$
26. $\operatorname{If} L^{-1}\{\bar{f}(s)\}=f(t)$ then $L^{-1}\{\bar{f}(s+a)\}=$ $\qquad$ [ ]
A) $e^{-a t} f(t)$
B) $e^{a t} f(t)$
C) $e^{a t}$
D) None
27. If $L^{-1}\left\{\frac{1}{s^{2}+a^{2}}\right\}=$
(A) $\frac{1}{a} \sin a t$
B) $\frac{1}{a} \cos a t$
C) $\sin a t$
D) $\cos a t$
28. Find the value of $L^{-1}\left\{\frac{1}{s^{2}-5 s+6}\right\}=$ $\qquad$
A) $e^{-3 t}-e^{-2 t}$
B) $e^{3 t}+e^{-2 t}$
C) $e^{3 t}-e^{2 t}$
D) None
29. $L\left\{c_{1} f_{1}(t)+c_{2} f_{2}(t)\right)=c_{1} L\left\{f_{1}(t)\right\}+c_{2} L\left\{f_{21}(t)\right\}$ This property in respect of Laplace transforms Is called
A) Shifting property
B) Distributive property
C) Symmetric property
D) Linearity property
30. $L\{1\}=$
A) $\frac{1}{s}$
B) $\frac{2}{s}$
C) $\frac{1}{s^{2}}$
D) 1
31. $L\left\{\frac{1}{\sqrt{t}}\right\}=$
A) $\sqrt{\frac{\pi}{s}}$
B) $\sqrt{\frac{1}{s}}$
C) $\sqrt{\frac{2 \pi}{s}}$
D) $\sqrt{\frac{s}{\pi}}$
32.If $L^{-1}\left\{\frac{s}{s^{2}+a^{2}}\right\}=$
(A) $\frac{1}{a} \sin a t$
B) $\frac{1}{a} \cos a t$
C) $\sin a t$
D) $\cos a t$
33.If $L^{-1}\left\{\frac{1}{2 s-5}\right\}=$
(A) $\frac{1}{2} e^{\frac{5 t}{2}}$
B) $-\frac{1}{2} e^{\frac{5 t}{2}}$
C) $e^{\frac{5 t}{2}}$
D) $\frac{1}{2} e^{\frac{2 t}{5}}$
32. If $L^{-1}\left\{\frac{1}{s^{n}}\right\}$ is a possible only when $n$ is
A)Positive integer
B) Zero
C) Negative integer
D) All of these
35.If $L^{-\prime}\{\bar{f}(s)\}=f(t)$ and then $\left.L^{-1}\left\{\int_{s}^{\infty} f \bar{s}\right) d s\right\}=$
A) $\mathrm{tf}(\mathrm{t})$
B) $\frac{f(t)}{t}$
C) $e^{a t} f(t)$
D)None
33. If $L^{-1}\{\bar{f}(s)\}=f(t)$ and $f(0)=0$, then $L^{-1}\{s \bar{f}(s)\}=$
A) $f^{\prime \prime}(t)$
B) $f(s)$
C) $f^{\prime}(t)$
D) $f^{1}(s)$ 37. $L\left\{5-3 t-2 e^{-t}\right\}=$
A) $\frac{3 s^{2}+2 s-3}{s^{2}}$
B) $\frac{3 s^{2}+2 s-3}{s^{2}(s+1)}$
C) $\frac{3 s^{2}+2 s-3}{s^{2}(s-1)}$
D) $\frac{3 s^{2}+2 s+3}{s^{2}}$
34. $L\left\{t^{3}\right\}=$
A) $\frac{6}{s}$
B) $\frac{6}{s^{3}}$
C) $\frac{6}{s^{2}}$
D) $\frac{6}{s^{4}}$
39.If $L^{-1}\{\bar{f}(s)\}=f(t)$ and $f(0)=0$, then $L^{-1}\{s \bar{f}(s)\}=$
(A) $f(t)$
В) $\frac{f(t)}{t}$
C) $\frac{f^{1}(s)}{s}$
D) $f^{1}(t)$
40.If $L^{-1}\{\bar{f}(s)\}=f(t)$ and $L^{-1}\{\bar{g}(s)\}=g(t)$, then $L^{-1}\{\bar{f}(s) . \bar{g}(s)\}=$
(A) $f(t) * g(t)$
B) $f(s) * g(s)$
C) $\frac{f(t)}{g(t)}$
D)None

## UNIT - II

1. The Fourier transform of a function $f(x)$ is
A) $\int_{0}^{\infty} f(x) e^{i p x} d x$
B) $\int_{-\infty}^{\infty} f(x) e^{i p x} d x$
C) $\int_{0}^{\infty} f(x) e^{-i p x} d x$
D) None
2.If $F\{f(x)\}$ and $G\{g(x)\}$ be the Fourier transforms of $f(x)$ and $g(x)$ then $F\{a f(x)+b g(x)\}=----$

Where $a$ and $b$ are constants
A) a $\mathrm{F}\{\mathrm{f}(\mathrm{x})\}+\mathrm{bF}\{\mathrm{g}(\mathrm{x})\}$
B) $(\mathrm{a}+\mathrm{b}) \mathrm{F}\{\mathrm{f}(\mathrm{x})+\mathrm{g}(\mathrm{x})\}$
C) $b \operatorname{F}\{\mathrm{f}(\mathrm{x})\}+\mathrm{aF}\{\mathrm{g}(\mathrm{x})\}$
D) None
3. The finite fourier sine transform of $f(x)=x$ in $(0, \pi)$ is $\qquad$
A) $\frac{\pi}{n}(-1)^{n+1}$
B) $\pi(-1)^{n+1}$
C) $\frac{\pi}{n}(-1)^{n}$
D) None
4. If $\mathrm{F}\{\mathrm{f}(\mathrm{x})\}=\mathrm{f}(\mathrm{p})$ then the inversion formula is $\qquad$
A) $\frac{1}{2 \pi} \int_{-\infty}^{\infty} f(p) e^{-i p x} d p$
B) $\frac{1}{2 \pi} \int_{-\infty}^{\infty} f(p) e^{i p x} d p$
C) $\frac{2}{\pi} \int_{-\infty}^{\infty} f(p) e^{-i p x} d p$
D) None
5. $F_{s}\left\{e^{-a t}\right\}=----$
A) $\frac{p}{\left(a^{2}+p^{2}\right)^{2}}$
B) $\frac{p}{a^{2}+p^{2}}$
C) $\frac{a}{a^{2}+p^{2}}$
D) None
6. If $F(p)$ is the Fourier transform of $f(x)$ then $F\{f(x-a)\}=$
A) $e^{i p a} F(p)$
B) $e^{-i p a} F(p)$
C) $e^{p a} F(p)$
D) $e^{-p a} F(p)$
7. Finite Fourier cosine transform of $f(t)=1,0<t<1$ is
A) $\frac{\sin n \pi}{n \pi}$
B) $\frac{\cos n \pi}{n \pi}$
C) $\sin n \pi$
D) $\cos n \pi$
8. If $F\{f(x)\}=F(p)$ then $F\{f(a x)\}=$
A) $a F\left(\frac{p}{a}\right)$
B) $\frac{1}{a} F\left(\frac{a}{p}\right)$
C) $a F\left(\frac{a}{p}\right)$
D) $\frac{1}{a} F\left(\frac{p}{a}\right)$
9. Find $F_{s}\left\{2 e^{-5 x}\right\}=$ $\qquad$
A) $\frac{2 p}{p^{2}+5^{2}}$
B) $\frac{5 p}{p^{2}+2^{2}}$
C) $\frac{p}{p^{2}+5^{2}}$
D) None
10. Fourier cosine transforms of $e^{-2 x}$ is
A) $\frac{p}{p^{2}+2^{2}}$
B) $\frac{2}{p^{2}+2^{2}}$
C) $\frac{-2 p}{p^{2}+2^{2}}$
D) $\frac{2 p}{p^{2}+2^{2}}$
11. Fourier sine transform of $\mathrm{f}(\mathrm{x})=\frac{1}{x}$ is ----
A) $\frac{\pi}{2}$
B) $\pi$
C) 0
D) None
12. For the function applying Fourier transform it has to satisfy $\qquad$
A) dirichlet
B)euler
C)parseval
D) $\frac{1}{z-1}$
13. If $F\{f(x)\}=f(p)$ then $F[f(x / a)]=$ $\qquad$
A) $\mathrm{f}(\mathrm{ap})$
B) $1 / \mathrm{a} \mathrm{f}(\mathrm{p} / \mathrm{a})$
C) a $\mathrm{f}(\mathrm{p} / \mathrm{a})$
D) None
14. Fourier cosine transform of $f(x)=e^{-x}$ is $\qquad$ [
A) $\frac{1}{1+p^{2}}$
B) $\frac{1}{1-p^{2}}$
C) $\frac{1}{p^{2}}$
D) None
15. Fourier cosine transform of $f(x)=X$ is
A) 0
B)1
C) $-1 / p^{2}$
D) None
16. $\operatorname{Find} F_{C}\left(f^{\prime}(x)\right)=$ $\qquad$
A) $-f(0)+F_{C}(P)$
B) $-f(0)+p F_{S}(P)$
C) $F_{C}(P)$
D)None
17. The fourier cosine transform of $\mathrm{f}(\mathrm{x})=\frac{e^{-a x}}{x}$ is $\qquad$
A) $\frac{1}{2} \log \left(P^{2}+a^{2}\right)$
B) $-\frac{1}{2} \log \left(P^{2}+a^{2}\right)$
C) $\frac{1}{2} \log \left(P^{2}-a^{2}\right)$
D)None
18. The fourier sine transform of $2 e^{-5 x}+5 e^{-2 x}$ is
A) $\frac{2 P}{P^{2}+25}+\frac{5 P}{P^{2}+4}$
B) $\frac{2 P}{P^{2}-25}+\frac{5 P}{P^{2}-4}$
C) $\frac{10}{P^{2}+25}+\frac{10}{P^{2}+4}$
D)None
19. $F_{S}\{x f(x)\}=$ $\qquad$
A) $-\frac{d}{d p}\left[F_{c}(p)\right]$
B) $\frac{d}{d p}\left[F_{S}(p)\right]$
C) $f(0)$
D)None
20. Find $\mathrm{f}(\mathrm{x})$ if its Fourier sine transform is $e^{-a p}$.
A) $\frac{2 P}{\pi\left(a^{2}+p^{2}\right)}$
B) $\frac{2 P}{\pi\left(a^{2}-p^{2}\right)}$
C) $\frac{2}{\pi}$
D)None
21. Fourier cosine transforms of $x e^{-a x}$
A) $\frac{a^{2}-p^{2}}{\left(a^{2}+p^{2}\right)^{2}}$
B) $\frac{a^{2}+p^{2}}{\left(a^{2}+p^{2}\right)^{2}}$
C) $\sqrt{2 \pi}$
D) None
22. If $F_{C}\{f(a x)\}=\mathrm{k} F_{c}\left(\frac{p}{a}\right)$ then $\mathrm{k}=$ $\qquad$
A) a
B) $\frac{1}{a}$
C) $a^{2}$
D)None
23. The Fourier cosine transform of $\mathrm{f}(\mathrm{x})=\left\{\begin{array}{c}k, \text { if } 0<x<a \\ 0, \text { if } x>a\end{array}\right.$
A) $\frac{K \sin a p}{p}$
B) $\frac{k \cos a p}{p}$
C) 0
D) 1
24. The Fourier sine transform of $\frac{e^{-a x}}{x}$ is
A) $\tan ^{-1} \frac{a}{P}$
B) $\tan ^{-1} \frac{P}{a}$
C) $\tan ^{-1} a$
D) $\tan ^{-1} P$
25. Find $F_{c}\{x f(x)\}=$ $\qquad$
A) $-\frac{d}{d p}\left[F_{c}(p)\right]$
B) $\frac{d}{d p}\left[F_{S}(p)\right]$
C) $f(0)$
D)None
26. The Finite Fourier sine transform of $f(x)=\frac{x}{\pi}$, in $0<x<\pi$ is
A) $(-1)^{n+1 / 2}$
B) $(-1)^{n-1 / 2}$
C) $(-1)$
D) $(-1)^{n+1} \frac{1}{n}$
27. The Finite Fourier sine transform of $f(x)=1$, in $0<x<\pi$ is
D) $\frac{1-(-1)^{n}}{n}$
28. The Finite Fourier cosine transform of $f(x)=1$, in $(0, \pi)$ is $F_{c}(n)=$
A) $\frac{16\left[(-1)^{n}+1\right]}{(n \pi)^{2}}$
B) $\pi$
C) $\frac{\left[(-1)^{n}-1\right]}{(n \pi)^{2}}$
D) 0
29. The Fourier sine transform of a function $f(x)$ is $F_{s}(P)=$
A) $\int_{0}^{\infty} f(x) \sin p x d x$
B) $\int_{0}^{\infty} f(x) \sin p x d p$
C) $\int_{0}^{\infty} F(P) e^{i p x} d x$
D) None
30. The finite Fourier cosine transform of $2 x$ in $(0,2 \pi)$ is
A) $\frac{(-1)^{n}}{n}$
B) $\frac{1-(-1)^{2}}{n}$
C) $\frac{\left[(-1)^{n}-1\right]}{(n \pi)^{2}}$
D) $\frac{8\left[(-1)^{n}-1\right]}{n^{2}}$
31. The Finite Fourier cosine transform of $f(x)=x$, in $(0,4)$ is $F_{c}(n)=$
A) $\frac{16\left[(-1)^{n}+1\right]}{(n \pi)^{2}}$
B) $\frac{1-(-1)^{2}}{n}$
C) $\frac{\left[(-1)^{n}-1\right]}{(n \pi)^{2}}$
D) $\frac{16\left[(-1)^{n}-1\right]}{(n \pi)^{2}}$
32. If $T$ is the period of $f(x)$ then the period of $f(a x+b)$ is
A) T
B) $\mathrm{T}-\mathrm{a}$
C) $\mathrm{T} / \mathrm{a}$
D) aT
33. $\mathrm{F}\{\mathrm{f}(\mathrm{x})\}=\mathrm{F}(\mathrm{p})$ then $F\{f(x) \cos a x\}=\frac{1}{2}[f(p+a)+f(p-a)]$ is
A) shifting theorem
B) linearity property
C) modulation theorem
D) None
34. The Inverse Fourier sine transform $F_{S}(P)$ is $f(x)=$
A) $\frac{2}{\pi} \int_{0}^{\infty} F_{S}(P) \sin p x d p$ B) $\int_{0}^{\infty} f(x) \sin p x d p$ C) $\left.\frac{2}{\pi} \int_{0}^{\infty} F_{c}(P) \cos p x d p \mathrm{D}\right)$ None
35. Fouier transform of the convolution of $f(x)$ and $g(x)$ is the product of their fourier Transforms is
A) Shifting theorem
B) linearity property
C) convolution theorem
D) None
36. The Fourier cosine transform of a function $e^{-a t}$ is
A) $\frac{P}{a^{2}+P^{2}}$
B) $\frac{a}{a^{2}+P^{2}}$
C) $\frac{-P}{1+P^{2}}$
D) None
37. $F_{c}\left(3 e^{-3 x}+2 e^{-4 x}\right)$ is
A) $\frac{2 P}{P^{2}+9}+\frac{5 P}{P^{2}+16}$
B) $\frac{2 P}{P^{2}-9}+\frac{5 P}{P^{2}-16}$
C) $\frac{9}{P^{2}+9}+\frac{8}{P^{2}+16}$
D)None
38. $F_{S}\left(e^{-2 x}+4 e^{-3 x}\right)$ is
A) $\frac{P}{P^{2}+4}+\frac{4 P}{P^{2}+9}$
B) $\frac{2 P}{P^{2}-9}+\frac{5 P}{P^{2}-16}$
C) $\frac{9}{P^{2}+9}+\frac{8}{P^{2}+16}$
D)None
39. $\int_{0}^{\infty} e^{a x} \cos b x d x=$
A) $\frac{1}{a^{2}+b^{2}}$
B) $\frac{c}{a^{2}+b^{2}}$
C) $\frac{b}{a^{2}+b^{2}}$
D) $\frac{a}{a^{2}+b^{2}}$
40. If $f(x)=\frac{2}{\pi} \int_{0}^{\infty} F_{c}(p) \cos p x d p$ is called
A) Inverse cosine transform
B) Inverse sine transform
C) Fourier transform
D) Fourier cosine transform

## UNIT III

## ALGEBRAIC STRUCTURES

1. The algebraic system ( $S, \circ$ ) is called $\qquad$ is the operation $o$ is associative
A) Group
B) Monoid
C) Semi group D
D) Abelian group
2. If $(I,+)$ is a Monoid where $I$ is the set of integers and + is the operation of addition Then the identity element is
A) 1
B) 0
C) -1
D) None
3. Let g be a homomorphism from ( $\mathrm{X}, \mathrm{o}$ ) to ( $\mathrm{Y}, *$ ). If $g: X \rightarrow Y$ is one-to-one and onto then $g$ is called
A) Bijection
B) Isomorphism
C) Epimorphism
D) Monomorphism
4. Let S be a nonempty set and $P(S)$ be its power set. The algebras $(P(S), \cup)$ and $(P(S), \cap)$ are
A) Monoid
B) Group
C) Abelian group
D) all
5. If the operations * is distribution over addition for any $a, b, c \in I$ then $a *(b+c)=\quad$ [ ]
A) $\left(a^{*} b\right) * c$
B) $a+\left(b^{*} c\right)$
C) $\left(a^{*} b\right)+(a * c)$
D)none
6. By cancellation law for any $a, b, c \in I$ and $a \neq 0 \quad a * b=a * c=>$
A) $b=c$
B) a
C) $a=c$
D)c
7. For $\mathrm{m}=1, \mathrm{f}: \mathrm{A} \rightarrow \mathrm{A}$ such an operation is called
A)unary operation
B) binary operation
C)m-nary operation D)none
8. For $\mathrm{m}=2, \mathrm{f}: \mathrm{A} \rightarrow \mathrm{A}$ such an operation is called
A)unary operation
B) binary operation
C)m-nary operation D)none
9. The operation * will be a binary operation on $G$ if and only if $\qquad$ $\forall \mathrm{a}, \mathrm{b} \in \mathrm{G}$
A) aeG
B) $b \in G$
C) $a^{*} b \in G$
D)none
10. The inverse of the identify element is the
A)inverse element
B) Identity element
C)idempotent element
D) nilpotent element
11. A group with addition binary operation is known as [ ]
A)Abelian group
B)Groupoid
C) subgroup
D)additive group
12. A group with multiplication binary operation is known as [ ]
A)Abelian group
B) additive group
C) multiplicative group
D)none
13. A group $G$ is said to be $\qquad$ if the commutative law holds [ ]
A)groupoid
B) semigroup
C)Abelian
D)none
14. In order word $(s, 0)$ is a semigroup if for any $x, y, z \in s$ then $x o(y o z)=$
A)(xoy)*z
B)(xoz)oy
C)(xoy)oz
D) $x^{*}\left(y^{*} z\right)$
15. semigroup isomorphism satisfies
A)on-to
B) one-one
C)one-one\&on-to
D)none
16. semigroupephimorphism satisfies
A) on-to
B)one-one
C)one-one\&on-to
D)none
17. Every homomorphic image of an abelian group is
A) sub group
B) semigroup
C)abeliangroup
D)none
18. If H is any subgroup of a group G then $\mathrm{HH}=$
A) $\mathrm{H}^{-1}$
B)e
C) 1
D) H
19. A non-empty subset H of a group ( $\mathrm{G},{ }^{*}$ ) a subgroup iff__where $\mathrm{a} \in \mathrm{H}, \mathrm{b} \in \mathrm{H}$
A) ab $\epsilon \mathrm{H}$
B) $a^{*} b \in H$
C) $a^{*} b^{-1} \epsilon H$
D) $a^{-1} b \in H$
20. An algebric structure ( $\mathrm{s}, *$ ) which has an identity element and also satisfies closure, associative law is called a
A)subgroup
B)groupoid
C)monoid
D)none
21. The identity element (if it exists) of any algebraic structure is
A)multiple
B)unique
C)one
D)zero
22. If $a^{*} e=a$ then $e$ is called $\qquad$ element for the operation
A)left identity
B)Right identity
C)identity
D)none
23. If $e^{*} a=a$ then $e$ is called $\qquad$ element for the operation
A)left identity
B)Right identity
C)identity
D)none

24 The nonzero set of integers under multiplication is
A)monoid
B) semigroup
C)Group
D) all
25. The order of the identity element of a group $G$ is
A) 1
B) 2
C) 0
D)3
26. The inverse of 4 in the multiplicative group of integers modulo 7 is
A) 3
B) 2
C) 4
D) 5
27. Associative law is
A) $\mathrm{AB}=\mathrm{B} \mathrm{A}$
B) $\mathrm{A}=\mathrm{A}$
C) $(\mathrm{AB}) \mathrm{C}=\mathrm{A}(\mathrm{B} \mathrm{C})$
D) $B=B$
28. The order of 4 in the group of addition modulo 12 is
A) 3
B) 7
C) 8
D) 10
29. The group with commutative is. $\qquad$ group.
A) an abelian
B) symmetric
C)alternating
D) commutative
30. If G is a group, H is a sub group of G and $\mathrm{a}, \mathrm{b} \in \mathrm{G}$, then the relation $\mathrm{a} \equiv \mathrm{b}(\bmod \mathrm{H})$ is [ ]
A)Reflexive
B) Symmetric C
31. The order of alternating group, if the set $S$ has $n$ elements is
A) $n$
B) n !
C) $n / 2$
D) $\mathrm{n}!/ 2$
32. The order of group of all one- one \& onto mappings from $S$ to $S$ there the order of $S$ is $n$, and is
A) n
B) n !
C) $n / 2$
D) $n!/ 2$
33. If G is a group and $\mathrm{a}, \mathrm{b} \in \mathrm{G}$, then $(\mathrm{ab})^{-1}=$
A) $a^{-1} b^{-1}$
B) $a b^{-1}$
C) $a^{-1} b$
D) $b^{-1} a^{-1}$
34. The solution of $a x=b$ in a group $G$, wherea, $b \in G$ is
A) $a b^{-1}$
B) $a^{-1} b^{-1}$
C) $a^{-1} b$
D) $a^{-1}$
35. If $e_{1}$ and $e_{2}$ are two identity elements of a group $G$, then
A) $e_{1}<e_{2}$
B) $e_{1}=e_{2}$
C) $e_{1}>e_{2}$
D) $e_{1} e_{2}$
36. If $G$ is a finite group of order $n$, and $a \in G t h e n$
A) $e^{n}=a$
B) $\mathrm{a}^{\mathrm{n}}=\mathrm{a}$
C) $a^{n}=e$
D) $a^{n} \neq e$
37.If the order of an element $a \in G$ is $n$ and the order of $a^{-1}$ is $m$,then
A) $m<n$
B) $m>n$
C) $m=n$
D) $m=a n$
38. The order of 4 in the additive group of integers $\bmod 6$ is
A)2
B) 3
C) 5
D) 4
39.The inverse of 8 in the multiplicative group of integers $\bmod 11$ is
A) 7
B) 9
C) 5
D) 6
40.If $G$ is a group and $a, b \in G$, then
A) $a^{2} b=a^{2} b^{2}$
B) $(a . b)^{2}=a^{2} \cdot b^{2}$
C) $a \cdot b=a^{2} \cdot b^{2}$
D) $a \cdot b \neq a^{2} b^{2}$

## UNIT IV

1. Enumerating r-permutations without repetitions $\mathrm{P}(\mathrm{n}, \mathrm{r})=$
А) $\frac{n!}{r!(n-r)!}$
B) $\frac{n!}{r!}$
C) $\frac{n!}{(n-r)!}$
D) None
2. How many 3 digit number can be formed using the digits $1,3,4,5,6,8$ and 9
A) $7 * 6 * 5$
B) 3 !
C) $\frac{7!}{3!}$
D) $7^{3}$
3. The series $1+\mathrm{x}+\mathrm{x}^{2}+$ $\qquad$ $=$
A) $\sum \mathbf{x}^{\mathrm{r}}$
B) $\sum(-1) x^{r}$
C) $\sum(-a)^{r} x^{r}$
D)none
4. If a student is to answer true or false questions and there are five questions, the number of ways, he can answer is
A) 10
B) 16
C) 32
D) 5
5. The number of two-digit words, if repetitions are allowed is
A) 576
B) 676
C) 52
D) 650
6. The four-digit numbers, that can be formed from the digits $1,2,3,4,5,6,7$ if there will be no repetitions are
A) 24
B) 6
C) 840
D) 120
7. The three-digit numbers, that can be formed from the digits $1,2,3,4,5$ if repetitions are allowed is
A) 125
B) 120
C) 60
D) 36
8. The number of ways sitting five people around a table is
A) 24
B) 120
C) 312
D) 720
9. The number of ways of drawing 2 cards with replacement from a deckof 52 cards is
A)2704
B) 1326
C) 52
D) 2652
10. The number of ways of drawing 2 cards without replacement from a deck of 52 cards Is
A)2704
B) 1326
C) 52
D) 2652
11. There are 12 red balls and 8 blue balls in a box. The number of ways of selecting 5 red balls and 3 blue balls is
A) 42126
B) 44352
C) 12118
D) 24352
12. The number of positive integer solutions of $x+y+z=6$ is
A) 24
B) 20
C) 10
D) 15
13. The three-digit numbers, that can be formed from digits $1,2,3,4,5$, if repetitions are not
allowed is
A) 125
B) 60
C) 45
D) 90
14. The number of non-negative integer solutions of $x+y+z=9$ is
A) 55
B) 45
C) 60
D) 72
15. The number of positive integer solutions of $x+y+z<7$ is
A) 20
B) 60
C) 120
D) 90
16. The number of permutations of the word SUCCESS is
A) 960
B) 420
C) 120
D) 840
17. The number of permutations of the word HAPPY is
A) 90
B) 120
C) 60
D) 40
18. The number of permutations of the word LAPTOP is
A) 240
B) 120
C) 360
D) 40030
19. The number of combinations of five objects among eight objects, if the repetitions are allowed and order is not important is
A) 645
B) 792
C) 896
D) 962
20. The number of combinations of three objects among six objects, if the repetitions are allowed and order is not important is
A) 56
B) 96
C) 48
D) 120
21. There are two groups; each consists of four questions each. If a student is to answer 2 from one group and 3 from another group, the number of ways that he can answer is
A) 48
B) 24
C) 72
D) 30
22. The coefficient of $x^{5} y^{2}$ in the expansion of $(x+2 y)^{7}$ is
A) 42
B) 84
C) 120
D) 96
23. The coefficient of $x^{5} y$ in the expansion of $(2 x+y)^{6}$ is
A) 192
B) 128
C) 120
D) 144
24. $|\mathrm{AUB}|=62,|\mathrm{~A}|=32,|\mathrm{~B}|=42$, then $|\mathrm{A} \cap \mathrm{B}|=$
A) 24
B) 15
C) 36
D) 12
25. The number of integers $<500$ and divisible by 3 or 6 or 7 is
D) 194
A)214
B) 248
C) 324
26. The number of integers $<250$ and divisible by 7 or 11 is
A) 54
B) 48
C) 74
D) 9
27. The co-efficient of $\left(x^{3}+x^{4}+x^{5}+---\right)^{5}$ is=----
A) 126
B) 127
C) 125
D)none
28. The solution of linear recurrence relation is ----methods
A) 4
B) 3
C) 2
D) none
29. Which method ,the solution is obtained as the sum of two parts----
A) substitution
B)characteristic root
C)step by step
D)none
30. When $\mathrm{fn}=0$, thentheequation is
is-----
A)homogeneous
B)non-homogeneous
C)none
31. If the characteristic equation has 2,1 roots, then the solution is----
A) $a_{n}=b_{1} 2^{n}+b_{2}(-1)^{n}$
B) $a_{n}=\left(b_{1}+2 b_{2}\right)(-1)^{n}$
C) $\left(2 b_{1}+(-1) b_{2}\right) r^{n}$
D)none
32. The solution of linear non-homogeneous equation is=------
D) none
33. $\sum a_{n} x^{n}$ is equal to
B) $a_{n}=A_{0}+A_{1} n+A_{2} n^{2}$
C) $\mathrm{Ab}^{\mathrm{n}}$
A) $\mathbf{a}_{0}+\mathbf{a}_{1} \mathbf{x}+\mathbf{a}_{2} x^{2}+-$
B) $a_{0} x+a_{1} x^{2}+a_{2} x^{3}+-$
C) $a_{0}+a_{1} X$
D)none
34. Solving recurrence relation for ----types
A) 2
B) 3
C) 1
D) none
35. The generating function of 1 is
A) $\frac{1}{1-x}$
B) $\frac{1}{1+x}$
C) $\frac{1}{1-2 x}$
D) $\frac{x}{1-2 x}$
36. The generating function of $3^{n}$ is
A) $\frac{x}{1-3 x}$
B) $\frac{x}{1+3 x}$
C) $\frac{1}{1+x}$
D) $\frac{x}{1-x}$
37. The generating function of $n$ is
A) $\frac{1}{1+x}$
B) $\frac{1}{1-x}$
C) $\frac{x}{(1-x)^{2}}$
D) $\frac{1}{(1-x)^{2}}$
38. The generating function of $1+\mathrm{n}$ is
A) $\frac{1}{1-x}$
B) $\frac{1}{1+x}$
C) $\frac{x}{(1-x)^{2}}$
D) $\frac{1}{(1-x)^{2}}$
39. The generating function of the sequence $1,-2,4,-8,16 \ldots \ldots$ is
A) $\frac{x}{1+2 x}$
B) $\frac{1}{1+2 \mathrm{x}}$
C) $\frac{x}{(1-x)^{2}}$
D) $\frac{x^{2}}{(1+2 x)^{2}}$
40. The exponential generating function of the sequence $1,1,1,1 \ldots \ldots$ is
A) $e^{x}$
B) $e^{-x}$
C) $e^{2 x}$
D) $e^{-2 x}$

## UNIT V

## GRAPH THEORY

1. A regular graph of degree $\qquad$ has no lines.
A) 0
B) 1
C) 2
D) 3
2. The maximum degree of any vertex in a simple graph with $n$ vertices is
A) $n$
B) $\mathrm{n}+1$
C) $\mathrm{n}-1$
D) $n+2$
3. A graph $G$ has 21 edges, 3 vertices of degree 4 and other vertices of degree 3. Find the number of vertices in $G$.
A) 10
B) 11
C) 12
D) 13
4. The maximum number of edges in a simple graph with $n$ vertices is
A) $n(n-1) / 2$
B) $(\mathrm{n}-1) / 2$
C) $n(n+1) / 2$
D) $n(n 1)$
5. A graph which allows more than one edge to join a pair of vertices is called
A) Simple graph
B) Multi-graph
C) Null graph
D) Weighted graph
6. A simple graph $G$, in which every pair of distinct vertices are adjacent is called
A) Simple graph
B) Multi-graph
C) Null graph
D)Complete graph
7. A binary tree $T$ has $n$ leaves. The number of nodes of degree 2 in $T$ is
A) $n-1$
B) n
C) $n+1$
D) $2 n$
8. The total number of edges of a complete graph $K_{n}$ is...
A) $n$
B) $\mathrm{n}^{2}$
C) $\frac{n(n+1)}{2}$
D) $\frac{n(n-1)}{2}$
9. A graph without edges is called a $\qquad$ .graph
A) trivial graph
B) null graph
C)infinite graph
D) simple graph
10. A graph is regular , if the degree of each vertex is $\qquad$ .
A) same
B) not same
C) always zero
D) always one
11. A graph $G$ has 21 edges, 3 vertices of degree 4 and other vertices of degree 3. Find the number of vertices in $G$.
A) 10
B) 11
C) 12
D) 13
12. The maximum degree of any vertex in a simple graph with $n$ vertices is
A) $n$
B) $\mathrm{n}+1$
C) $\mathrm{n}-1$
D) $n+2$
13. Eular's rule is
A) $v+e+r=2$
B) $v-e+r=2$
C) $\mathrm{ve}-\mathrm{r}=2$
D) $v+e r=2$
14. A planar graph has only $\qquad$ infinite region(s).
[ ]
A) one
B) two
C) Three
D) four
15. If a connected planar graph $G$ has e edges, $v$ vertices and $r$ regions, then
[ ]
A) $v+e+r=2$
B) $\mathrm{v}-\mathrm{e}+\mathrm{r}=2$
C) ver=2
D) $v+e r=2$
16. A connected graph that contains an Euler Circuit is called
A) Euler trail
B) Semi-Euler graph
C) Euler graph
D) Hamilton graph
17. A complete bipartite graph $\mathrm{K}_{\mathrm{m}, \mathrm{n}}$ is planar if and only if
A) $m>3$ or $n>3$
B) $m<3$ or $n>3$
C) $m<=3$ or $n<=3$
D) $m>=3$ or $n>3 b$
18. A graph $\mathrm{G}=(\mathrm{V}, \mathrm{E})$ is called a $\qquad$ graph if its vertices V can be partitioned into twosubsets $V_{1}$ and $V_{2}$ such that each edge of $G$ connects a vertex of $V 1$ to a vertex of $V 2$
A) simple
B) bipartite
C) complete bipartite
D) multi graph
19. The chromatic number of completebipartite graph is $\qquad$
A) 1
B) 2
C) 3
D) 0
20. A complete graph with $n$ vertices will have $\qquad$ edges
A) $(n-1)(n-2) / 2$
B) $n(n-1) / 2$
C) $(\mathrm{n}-2) / 2$
D) $n(n-2) / 2$
21. A graph which allows more than one edge to join a pair of vertices is called a
A) simple graph
B) null graph
C) multi graph
D) Pseudo graph
22. If $G$ is a connected graph with $n$ vertices and $m$ edges, a spanning tree of $g$ must have_ $\qquad$
A) $n$
B) $n+1$
C) $n+3$
D) $\mathrm{n}-1 \quad[\quad]$
23. A given connected graph is a Eular graph if and only if all vertices of $G$ are of
A) same degree
B) even degree
C) odd degree
D) Different degree
24. An $\qquad$ through a graph is a path whose edge list contains each edge of the graph exactly once.
A) Eular path
B) Eular circuit
C) Eular graph
D) Eular region [ ]
25. An $\qquad$ is a graph that possesses a Eular circuit.
A) Eular path
B) Eular circuit
C) Eular graph
D) Eular region
26. A circuit in a connected graph which includes every vertex of the graph is known as [ ]
A) Eular
B) Universal
C) Hamiltonian
D) Clique
27. If G is agraph within vertices, then a Hamiltonian cycle in G will contain exactly $\qquad$ edges
A) $n-1$
B) n
C) $n+1$
D) $n+2$ [
]
28. The length of a Hamiltonian path in a connected graph of $n$ vertices is
A) $n-1$
B) $n$
C) $n+1$
D) $n+2$
29. A circuit in a connected graph which includes every vertex of the graph is known as
A) Eular
B) Universal
C) Hamiltonian
D) Clique
]
30. The number of colors required to properly color the vertices of every planar graph is
A) 2
B) 3
C) 4
D) 5
31. The vertices of a planar graph with less than 30 edges is $\qquad$ colorable
A) 1
B) 2
C) 3
D) 4
32. A simple connected planar graph with 17 edges and 10 vertices cannot be $\qquad$ colorable
A) 1
B) 2
C) 3
D) 4
33. The chromatic number of an isolated vertex is
A) one
B) two
C) three
D) four
34. The Chromatic number of a graph having atleast one edge is atleast
A) one
B) two
C) three
D) four
35. Every $\qquad$ graph is 5colorable
A) simple
B) bipartite
C) planar
D) Euler
